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# Data Embedding in Digital Media

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Optimal Spread -Spectrum and  
Least-Significant -Bit Methods

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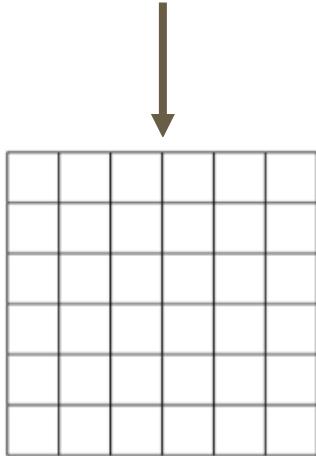
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# Project Summary

- Steganography
- Digital Steganography
- Least-Significant Bit Method
- Optimal Spread Spectrum Method



# OSS Algorithm Summary



01010001011

Embedding



01010001011

Recovery



Transmission

# Math

1. Auto -Correlation Matrix
2. Calculate Eigenvectors and Values
3. Calculate S\_opt and C\_opt
4. Calculate A values
5. Calculate Projection Matrix

Embedding Equation

$$Y = SAB + TX + N$$

Output      Amplification      Pattern  
Hidden bits      Projection Matrix      Transformed Image  
Noise

Equations :

$$R = TX * TX' / \text{size}(TX, 2)$$

$$[Q, \lambda] = \text{eigsort}(R)$$

$$S_{\text{opt}} = Q(1:k)$$

$$C_{\text{opt}}(k) = (\lambda(k) + \sigma^2 + D - \sqrt{(\lambda(k) + \sigma^2 + D)^2 - 4\lambda(k)*D}) / (2\lambda(k))$$

$$A(k) = \sqrt{D - c(k)^2 \lambda(k)}$$

$$T = \text{eye}(L) - S * C * S'$$

# Comparison

## Optimal Spread Spectrum

- Works with lossy compression
- Harder to detect with steganalysis
- Works with additive noise

## Least Significant Bit Replacement

- No bit errors (lossless compression)
- 4 -12 times more storage
- No recovery key
- Computationally faster
- Less distortion

# References

M. Gkizeli, D. A. Pados, and M. J. Medley, "Optimal signature design for spread  $\alpha$ -spectrum steganography," IEEE Trans. Image Process., vol. 16, pp. 391 -405, Feb. 2007.

Ming Li, Ngwe Thawdar, Dimitris A. Pados, Stella N. Batalama, and Michael J. Medley, "Minimum  $\alpha$ -Distortion Data Embedding in Video Streams" IEEE ICC 2014.